

Name: _____

Date: _____

Math 10/11 Enriched: Section 5.4 Solving Systems of Equations with Radicals

1. For what value(s) of “k” will the equation have an extraneous root?

i) $\sqrt{13x-1}=k$

ii) $3\sqrt{5x+1}+4+k=0$

2. When given an equation in the form $3x+b=\sqrt{5x+c}$, how do you tell if an answer is an extraneous root or not? Explain why extraneous roots exists.3. Suppose you are given the equation $4x-12=3\sqrt{6x^2-8x+b}+3$ with an answer of $x=2$, is this answer an extraneous root? Explain:4. When graphing $y=a\sqrt{bx-c}+d$, how do you know whether if the graph is opening UP or DOWN, LEFT or RIGHT? Explain:

5. Solve for “x”. Indicate any extraneous roots and restrictions on the domain:

a) $\sqrt{x}=5$	b) $2\sqrt{x+1}=5$	c) $\sqrt{3x+1}=16$
d) $-3\sqrt{4x-1}=-2$	e) $15+\sqrt{4x-3}=9$	f) $\sqrt{2x+25}=\sqrt{x+14}$

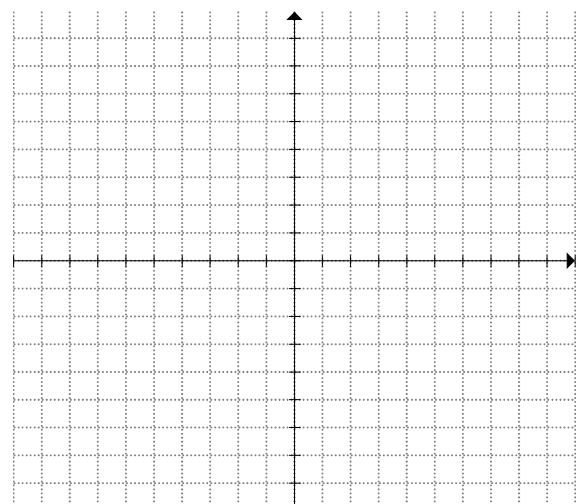
$$g) \sqrt{x} = x + 3$$

$$h) \sqrt{3x+1} = 2x-6$$

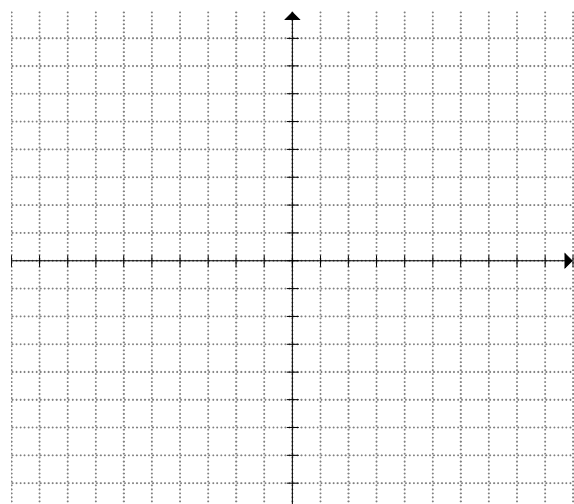
$$i) 3\sqrt{3x+1} = -(x+5)$$

6. Graph the system with the left side as Y1 & right side as Y2. Solve the system by finding all intersection points

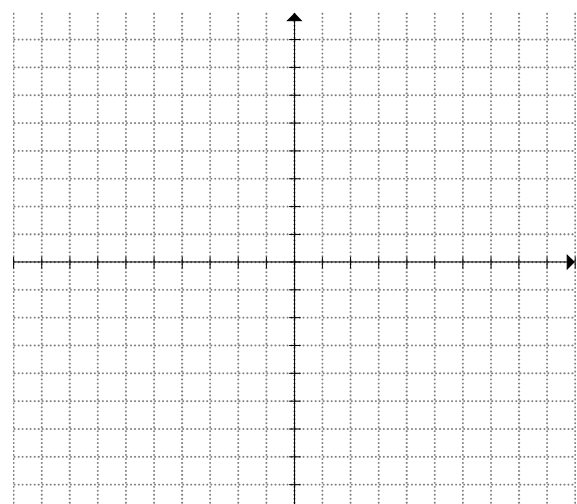
$$a) \sqrt{x+5} = -x-5$$



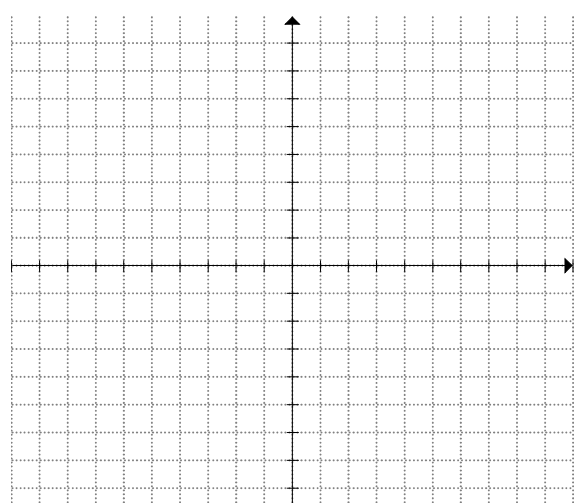
$$b) \sqrt{3x+1} = x-9$$



$$c) \sqrt{-x} = \frac{x}{x+2}$$



$$d) \sqrt{\frac{37}{2}\left(\frac{x}{3}+1\right)} = \frac{1}{(x+2)^2}$$



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7. Solve each of the following equations. Indicate an extraneous roots:

a) $\sqrt{x+2} = \frac{1}{\sqrt{x+2}}$

b) $\sqrt{x^2-8} = \sqrt{3x+2}$

c) $\sqrt{x^2+3} = x+1$

d) $\sqrt{x-2} = 4-x$

e) $\sqrt{2x+3} - \sqrt{x+2} = 2$

f) $\sqrt{x-8} + \sqrt{x} = 2$

g) $\sqrt{x} + \sqrt{x-3} = 9$	h) $\sqrt{x-2} + \sqrt{3x-3} = 3$
i) $\sqrt{x+6} = \frac{2}{\sqrt{x+1}} + \sqrt{x+1}$	f) $\frac{3}{\sqrt{x}} - 5 = \frac{1-2\sqrt{x}}{\sqrt{x}}$

8. Solve for all real value(s) of "x" $\sqrt{x+10} - \frac{6}{\sqrt{x+10}} = 5$

9. Find all "z" such that $\sqrt{5z+5}-\sqrt{3-3z}-2\sqrt{z}=0$

10. It so happens that $\sqrt{1800}+\sqrt{200}=\sqrt{n}$, where "n" is an integer. What is the value of "n"?

11. Find all real values of "x" which satisfy $\sqrt{x^2+1}+x^2+1=90$

12. Find $2x+5$ if "x" satisfies $\sqrt{40-9x}-2\sqrt{7-x}=\sqrt{-x}$



13. Evaluate the expression. No Calculator: $\sqrt{3+2\sqrt{2}} - \sqrt{3-2\sqrt{2}} = ?$

14. Solve for "x" $\sqrt{x+\sqrt{x+11}} + \sqrt{x-\sqrt{x+11}} = 4$

15. Determine the sum of the solution for "x": $\sqrt{2x-7} = 2 + \sqrt{x-7}$

16. Determine the domain of the following function: $y = \sqrt{190 - \sqrt{x}}$

17. For how many real values of "x" is $\sqrt{2211 - \sqrt{x}}$ an integer?

18. Given the two expressions, determine which one is bigger. Provide a proof to justify your answer:

$$\sqrt[n]{n!} \text{ vs } \sqrt[n+1]{(n+1)!}$$

19. If $\sqrt{\frac{3}{1} \times \frac{5}{3} \times \frac{7}{5} \times \dots \times \frac{2n+1}{2n-1}} = 9$, then what is the value of "n"? Fermat #21

20. What are all real values of "x" which satisfy:

$$\sqrt{x + 2\sqrt{x-1}} + \sqrt{x - 2\sqrt{x-1}} = 2\sqrt{x-1} \text{ ?}$$

21. IF $S = \sqrt{\frac{a}{b}}$, where "a" and "b" are both primes, find $a+b$ =??

$$\text{Let } S = \sqrt{9 - \sqrt{\frac{13}{9} + \sqrt{\frac{13}{81} - \sqrt{\frac{13}{6561} + \sqrt{\frac{13}{43046721} - \dots}}}}}$$

22. A student mistakenly thinks that the equation below is correct: $\sqrt{a^2 + b^2} = \sqrt{a^2} + \sqrt{b^2}$

Find as many ordered pairs of integers (a,b) such that $-10 \leq a \leq 10$ and $-10 \leq b \leq 10$, and that satisfies the equation: $\sqrt{a^2 + b^2} = \sqrt{a^2} + \sqrt{b^2}$: Brilliant.org